The Crystal and Molecular Structure of Phosphorus Thioiodide

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The crystal structure of phosphorus thioiodide has been determined by means of electron-density projections on to the (100) and (010) planes. The crystals are triclinic, space group $P\overline{1}$ with cell constants

a = 7.31 Å, b = 7.35 Å, c = 19.61 Å; $\alpha = 94^{\circ} 24'$, $\beta = 90^{\circ} 10'$, $\gamma = 90^{\circ} 55'$.

There are four molecules, of composition $P_4S_3I_2$, in the unit cell, two crystallographically independent molecules forming the asymmetric unit. The approximate iodine coordinates were found as a result of direct determination of the signs of a number of (0kl) and (h0l) structure factors by the application of Harker Kasper inequalities and of sign relationships.

The $P_4S_3I_2$ molecule consists of two five-membered rings of three phosphorus and two sulphur atoms, joined by a common P–S–P angle, the iodine atoms being bonded to phosphorus atoms of different rings. The molecule has twofold rotation symmetry. Iodine coordinates and phosphorus (and sulphur) coordinates have been determined with standard deviations of 0.01 Å and 0.03 Å respectively, and observed bond lengths and angles are compared with those in the phosphorus sulphides and iodides.

1. Introduction

The existence of three phosphorus thioiodides, of composition $P_4S_3I_2$, PSI and P_2SI_4 respectively, together with several methods for their preparation were reported by Ouvrard (1892, 1894). An attempt to confirm these reports and to determine the interrelationships of the compounds was made recently in this department by Topsom & Wilkins (1956). They found that PSI and P_2SI_4 could not be prepared by the methods given and consider that their existence is open to serious doubt. It appears therefore that $P_4S_3I_2$, which is readily prepared, is probably the only thioiodide formed by phosphorus. An ebullioscopic molecular weight determination in carbon disulphide showed that this compound is monomeric.

A knowledge of the molecular configuration of $P_4S_3I_2$ was considered to be of interest, particularly with a view to comparisons with the known configurations of the phosphorus sulphides P_4S_{10} and P_4S_7 (Vos & Wiebenga, 1955), P_4S_5 (van Houten & Wiebenga, 1957), P_4S_3 (Leung, Waser *et al.*, 1957). The molecular configurations reported show that the arrangement of phosphorus and sulphur atoms in these molecules is remarkably flexible and difficult to predict. More than one chemically reasonable molecular configuration could be postulated for $P_4S_3I_2$ but there was no experimental evidence for distinguishing them prior to this investigation. The crystal structure, leading to the molecular structure was found directly by X-ray crystallographic analysis.

2. Experimental

Phosphorus thioiodide was prepared by mixing white phosphorus, sulphur and iodine as their solutions in carbon disulphide (Topsom & Wilkins, 1956) and purified by recrystallization from this solvent at -78 °C., crystals of a size suitable for X-ray examination being obtained by controlled evaporation at room temperature. Invariably the crystals were found to be twinned on (001) but a few of them could be cleaved to give untwinned fragments. During recording of the diffraction data the crystals, which decompose fairly readily in moist air, were sealed in Lindemann glass capillaries.

Crystallographic data

Phosphorus thioiodide, $P_4S_3I_2$, m.p. 118 °C. with decomposition. The crystals are triclinic with

$$\begin{array}{l} a = 7 \cdot 31 \pm 0 \cdot 01, \quad b = 7 \cdot 35 \pm 0 \cdot 01, \quad c = 19 \cdot 61 \pm 0 \cdot 03 \text{ Å}, \\ \alpha = 94^{\circ} \cdot 24', \quad \beta = 90^{\circ} \cdot 10', \quad \gamma = 90^{\circ} \cdot 55'; \quad \text{all} \pm 10'. \\ (\text{Cu } K\alpha, \lambda = 1 \cdot 542 \text{ Å}). \end{array}$$

Density observed by flotation, $3 \cdot 0 \pm 0 \cdot 1$ g.cm.⁻³; calculated for four molecules per unit cell, $3 \cdot 04$ g.cm.⁻³. The linear absorption coefficient for Cu $K\alpha$ radiation is 625 cm.⁻¹; for Mo $K\alpha$ radiation 77 cm.⁻¹. The application of a statistical test (Howells, Phillips & Rogers, 1950) to the ($\hbar 0l$) intensities indicated the presence of a centre of symmetry. The probable space

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group was therefore $P\overline{1}$ with two $P_4S_3I_2$ molecules constituting the asymmetric unit, and this was confirmed by the structure analysis.

Relative intensities of (h0l) and (0kl) reflections were obtained for both Cu $K\alpha$ and Mo $K\alpha$ radiation by use of standard Weissenberg techniques and visual comparison of spots with intensity scales. (1kl) intensities were derived from Mo $K\alpha$ radiation only. In the final refinement of atomic coordinates, the more accurate Mo $K\alpha$ data were used, obtained from crystals measuring approximately 0.2 mm. in each axial direction. These data comprised 258 (h0l) reflections (68% of the possible to a limiting $\sin \theta/\lambda$ value of 0.65) and 184 (0kl) reflections (60% of the possible to a limiting $\sin \theta/\lambda$ value of 0.58). No absorption corrections were made.

3. The approximate iodine positions

The essential problem in this structure analysis was the determination of the positions of the four crystallographically independent iodine atoms, for it was calculated by the method of Sim (1957) that 82-84%of all structure factors would have the same sign as their total iodine atom contributions (as compared with 84% found when refinement ceased). Iodine coordinates could not be determined from the Patterson projections P(v, w) and P(u, w) which were evaluated. Neither of these projections could be interpreted uniquely, partly because of the extent of the overlap of I-P and I-S type vectors.

The presence of several outstandingly strong (0kl)reflections suggested the use of Harker Kasper inequalities (e.g. Harker & Kasper, 1948; Kasper, Lucht & Harker, 1950) to determine directly the signs of structure factors. As four of the unitary structure factors U(0kl) were greater than 0.6, many sign relationships could be deduced. The signs of 59 structure factors were established in terms of three variables (which were the unknown signs of three large structure factors), while use of the sign relationship $s(\mathbf{H}) =$ $s(\mathbf{H}')$, $s(\mathbf{H} + \mathbf{H}')$, which is probably true for combinations involving only large structure factors, (Cochran, 1952; Cochran & Woolfson, 1955) established as probable a further 61 signs in terms of the same three variables although 9 of these probable signs were later shown to be wrong. By similar methods the signs of 25 (h0l) structure factors were proved and a further four established as highly probable, this time in terms of only two variables.

The (h0l) Fourier syntheses for the four sign combinations of the two variables were computed, including in the summation only the 29 terms whose signs were established. The correct partial electrondensity projection on (010) was readily identified by consideration only of possible iodine peaks. The approximate iodine coordinates so obtained were used to determine more signs, including those of a number of (00l) reflections, and with aid of these latter signs, the correct combination of the variables for the (0kl) structure factors was found. A Fourier synthesis with known (0kl) terms was then computed and from the resulting partial electron-density projection on (100) the iodine peaks were readily identified.

4. Refinement of atomic coordinates

Refinement of the structure proceeded using Fourier and difference Fourier techniques, for both (100) and (010) projections. Initially signs of structure factors were regarded as determined only by large contributions of the iodine atoms. Most of the 14 phosphorus and sulphur atoms were located using the $\hat{C}u K\alpha$ data and all were clearly defined following extension of the refinement with Mo $K\alpha$ data.

In the (100) projection there were strong indications from difference maps that the iodine atoms were vibrating anisotropically, all four in the asymmetric



Fig. 1. Electron-density projections of the asymmetric unit (a) on (010), (b) on (100). Contours at an interval of 4 e.Å⁻² for P and S, 12 e.Å⁻² for I atoms, starting at 8 e.Å⁻². Final atomic positions indicated by black dots.

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Table 1. Observed and calculated structure factors

hkl	Fo Fc	hkl	P _o F _c	hkť	Fo Fc	hkł	Fo Fc	hkł	Fo Fo	h k ł	Fo	F _c hk	l Fa	o Fe	h k (Fo Fe	h k l	Fo Fc
0,0,0	7* ⁸⁵⁷	2,0,0	16 6 64 56	3,0,6	71 64- 78 79	5,0,16	37 36-	7,0,12	40 38	0,1,0	11*	1- 0,2	7 20	20-	0,4,14	29* 37	0,6,8	94 93-
2	36 34-	. 2	109 109	8 9	197 258	18	25* 2-	14	26 18	- 2	17	19-	9 118	2 205 B 107	16	51 55-	10	31* 11-
, í	156 172-	. <u>í</u>	153 166-	10	18* 5-	20	26* 18-	16	20* 28 27* 2	- 4	133	128 · 172 ·	10 115	5 112	17	32* 25- 39 45-	11	32 41 32* 21
5	11* 1- 173 191-	. 6	27 10-	12	103 103-	5.0.1	88 87	17	27* 17	5	203	230-	2 10	6 107	19	34× 11	13 14	33★ 13 34★ 19
7	13* 5-	. 7	130 122 81 72	14	26 39-	2	9 <u>3</u> 86	7,0,1	91 99 22 + 13	7	18*	2-	13 25 14 194	5★ 18 L 221-	0,4,1	148 146	15	34* 21
9	27 23	10	43 22	16	115 125-	រ្ន៍	120 139-	3	μi μo	- 9	36	50	15 26	6 * 17	23	121 115- 133 130-	0,6,1	27* 22
10	227 252 33 30-	. 11	59 43	18	74 94	Ğ	22 0	5	55 47	- 10	27 70	35 70	17 29	9 * 11	4	45 42- 22* 5-	. 2	106 101- 27 * 22
12	94 87- 28 32	13	141 149-	19 20	24★ 0 34 34	ģ	20* 20	67	23* 17 23* 2	12	23	25-	18 30	0★ 25 1★ 20-	é	114 101	45	77 64
14	19* 1-	14	28 31	21 22	25 20 35 21-	10	20+ 10	8	56 59 20+ 16	- 14	Ϊų́	40	20 32	2* 1 3* 3-	8	102 91	Ğ	28* 6
16	79 78-	16	39 39- 21★ 10-	23 24	26* 19- 27* 9-	12	42 46	10	24* 22	- 16	48	55 -	22 31	4* 37	10	25* 12 25* 10-	. 8	40 45
17	21* 20- 21* 13	· 18	41 36 23* 19	4.0.0	72 69-	13	27 19 63 54-	12	25* 18	- 17	28★ 30★	17- 0,3	,0 58	8 40	11	46 45	. 10	100 95 56 48-
19	22* 1-	20	24 26	. 1	117 122-	15 16	75 84- 127 121	13	31 30 37 25	- 19	31	34-	2 19	9 197	13	133 135-	. 11	30 * 26- 72 67-
21	24* 16-	. 22	25* 8	3	30 15	17	24 ± 1- 25 ± 30-	15	35 48 27+ 23	21	42	50	3 7	1 65- 2 56-	14	29 * 10	13	31 * 31-
23	29 30	24	27* 21-	5	22 2	19	26* 7	17	27★ 9		54 *	15-	5 94	4 103	16	30★ 3- 30★ 30	15	52 45-
24 25	26★ 13 27★ 3-	2,0,1	40 27	ž	130 140	21	27* 11	8,0,0	· 24* 5	- 0,1,1	31 38	19 24	7 218	8 229-	18	85 89	16 17	33★ 23 34★ 33
1,0,0	25 24	3	178 203	ŝ	59 57-	6,0,0	119 129-	2	24 * 20	- 4	40 147	25 141-	9 7	7 94-	20	33* 35	0.7.0	57 40
1	35 28 40 22-	. 5	127 103- 138 149	11	22 8-	23	91 83 23 19	3 4	46 50 67 79	5	141	142-	10 22	4* 12 0 151	0,5,0	24 15	1	30* 20 30 35-
3	171 196-	. 6	125 127-	13	39 30-	1 <u>5</u>	72 69 39 24	5	70 61 25★ 5	- 7	38	34	12 20	6* 12- 7* 17	2	69 56	. 3	<u>43</u> <u>43</u>
5	143 155	8	190 214	15	20 28-	6 7	40 37- 35 34-	7	70 76	9	71	62	14 20	8 47-	34	191 220 85 80-	. 5	31 32
7	52 50-	10	20 20-	iž	88 110	8 9	74 68- 27 35	.9	26+ 15	- 10	38 42	41	16 30	6 41-	5	26* 6 26* 9-	. 7	31★ 3 32★ 6
ŝ	132 138-	12	22 9	19	25* 10 25* 8-	10	101 110- 26 29	11	26* 13	12	106	129 79-	17 5	2 37	7	57 71-	. 8	32* 8~ 33* 37~
10	52 46 56 50	14	43 31-	21 22	26 28- 26* 11-	12 13	86 108 24* 1-	12	26* 34 56 70	- 14	25 *	18	19 3 20 31	3★ 27- 4★ 28	9	28* 4	10	33* 9- 34* 10-
12	43 41 18 6	15	60 63-	23	27* 40-	14	45 33 25* 24-	14	27* 24	16	27	43 0.3	.1 80	0 76	11	29* 20	12	34* 13-
14	109 125	18	68 63	4,0,1 2	60 63- 118 120-	16 17	34 29 26* 33-	8,0,1	57 62 45 42	18	50	58-	2 3	5 30	12	30 * 18 73 84	0,7,1	65 51-
16	74 88-	20	24* 11-	Ę.	131 134 17* 18-	18	29 18 27* 7	34	24 ± 11 24 ± 1	- 19	50 31★	8	4 19	2 17	14 15	31★ 17- 32★ 2	. 3	30 * 6
18	39 47-	21	25* 5 25 32	ŝ	110 103-	20	51 55-	56	46 34	- 21 22	32★ 34★	28 4-	6 Ψ	4 39-	16 17	33* 28 34* 19	. 5	30* 11- 30* 19
19 20	25 6- 23* 21	23	41 50 28 21-	á	45 49	6,0,1 2	20 2- 20* 6	Ž	38 35	0.2.0	15	14-	8 30	1 60- 6 30	051	84 63-	. 7	56 59 31* 14
21 22	35 31- 25* 12-	3,0,0	55 44	10	64 66-	4	50 46- 43 41-	Jõ	25* 10	-,-,i	89	81 .	9 200 10 44	8 197 4 35-	2	24 27	89	31★ 21- 31★ 7-
23 24	26★ 20- 26★ 21	1 2	14 * 11 163 176	12	74 65-	5	41 31 86 83	11	26* 20	3	15*	2-	11 9 12 5	7 86- 0 43	4	25* 1-	10	55 31
25	32 32	34	14* 6 123 125-	14	21* 18-	7	21 * 10 93 90	13	27* 33	- 5	34	38-	13 8	7 62- 7± 15	26	71 60	12	33* 15-
1,0,1	104 103- 91 91-	5	33 22- 86 86	16	80 81	10	102 99-	14	2/* 0	7	26	28	15 20	8 22	7	143 135 26* 7	14	34 * 21-
34	74 58 34 29-	7	16* 0 206 246-	18	群* 部-	12	23* 11-	9,0,0	37 38	- 8	36 22	23-	17 3	56-	9 10	88 73- 28* 15	0,8,0	33 * 7-
5	172 188 90 78	10	46 28	20 21	25* 5- 26* 18	14	24* 16	3	26 * 10	- 10	23 85	30- 102	19 7	5 73	11	43 53	1	55★ 4 33★ 20-
7	13 7-	11	18* 12	22 23	26* 14- 27* 27	16	46 58	4 5	27 40 26* 20	12	73	82 56-	20 3 21 31	3★ 18 4 33-	12	61 52-	. <u>3</u>	42 47 50 55
9	63 59 16 * 7	13	20* 13-	5,0,0	.34 .27-	18	26 12	67	27* 11 27* 15	14	26*	13-	22 4	8 40	14	30* 26-	- 5	34* 9
11	175 183-	15	21 * 4-	2	40 43	żó	51 52-	89	27 * 1 27 * 6	16	36	38- 0,4	,0 2	2* 17-	16	40 28-	·	70 77
13	38 34	17	31 23- 74 87-	4	66 66	7,0,0	22* 7-	9,0,1	41 43	- 18	30	37	2 7	5 59	17	98 78 33* 16	2	33★ 8-
15	61 54	19	24 12 46 55	56	76 84-	2	30 29-	3	26 * 6	- 20	48 33*	47-	4 2	3* 12	19	48 62-	. 3	ე8 40- 33★ 26-
17	30 14-	21	25* 12 45 50	8	61 88 30 21	ų	22 34	45	27 22	21	34*	17	2 2	_و2 د _و_ ★µ	0,6,0	27* 6-	. 5	33 30- 67 75
19	40 02 44 57	23 24	26 * 3 27 * 2	10	20 25- 20 18-	261	39 37	7	0ر ور 17★ 17	- ^{0,2,1}	139 51	120-	/ 7 [.] 8 2	1 67− 5 x 1-	2	35 29	Ž	34* 19 58 56-
20	23 * 10 57 80-	3,0,1	.26 .12	11 12	61 57 29 39	8	25* 22- 37 31	8 9	27* 20 27* 25	- 3	69	57	9 8 10 2	9 83 6 28-	34	28* 0 28* 6	9	55 42
22	26 ★ 31-	23	147 151-	13	46 39-	9 10	79 91 24 28-	,		5	115	99-	11 2 12 A	7* 32~ 3 74	56	67 56 62 68	-	
24	45 51- 27* 12	· 45	97 82-	15	90 103-	11	24 13-			6	25	24-	13 2	9* 12-	7	64 59	-	

* Minimum observable amplitude for unobserved reflection.

unit having approximately the same direction of maximum vibration. They were finally assigned a temperature factor of the form

 $\exp\left[-\left\{2\cdot9+8\cdot0\sin^2\left(\varphi-\psi_c\right)\right\}\sin^2\theta/\lambda^2\right],$ (Hughes, 1941; Cochran, 1951)

where $2 \sin \theta$, φ are the polar coordinates of a point in the reciprocal lattice 0kl, and where ψ_c , the angle between the direction of maximum vibration and the c axis, is 39°. The values of the isotropic thermal parameter B (in the expression exp $(-B \sin^2 \theta / \lambda^2)$) for the phosphorus and sulphur atoms in this projection were 1.5 and 2.3 respectively. In the (010) projection no significant anisotropy was apparent, isotropic thermal parameters for iodine, phosphorus and sulphur atoms being 2.9, 1.2 and 2.1 respectively. Atomic scattering factors used were those of Thomas & Umeda (1957) for iodine, and Viervoll & Øgrim (1949) for phosphorus and sulphur. The final electron-density projections are shown in Fig. 1, and observed and calculated structure factors are compared in Table 1. The final values for the reliability factors were R(0kl) = 0.12 and R(h0l) = 0.14 for all observed reflections.

The two-dimensional refinements led to a location in space for each atom and hence enabled the molecular configuration to be deduced unequivocally. The phosphorus and sulphur atoms were distinguished solely on chemical grounds on the assumption that their valencies are three and two respectively. It was then observed that the two sets of atoms did in fact have significantly different temperature factors. The three coordinates finally assigned to each atom (the common z coordinates being averaged) were used to calculate 89 (1kl) structure factors with values of sin θ/λ up to 0·3. For the purpose of these check calculations, isotropic thermal parameters were given values $3\cdot 2$ and $1\cdot 32$ for iodine atoms and all light atoms respectively, so that the calculations were not exact. Never-

	\boldsymbol{x}	3J	z	X'	Y'	Z'
Molecule (1)		Ū				
I,	0.607	0.950	0.0973	4·326 Å	6·952 Å	1·375 Å
$\mathbf{I_2}^{-}$	-0.106	0.287	0.2075	-0.809	2.101	3.908
\mathbf{P}_{1}	0.398	0.718	0.043	2.83	5.25	0.44
P,	0.423	0.519	0.123	3.03	3.80	2.12
P_3	0.049	0.716	0.157	0.27	5.24	2.68
$\mathbf{P_4}$	-0.032	0.457	$0.102_{(5)}$	-0.32	3.34	1.75
S ₁	0.130	0.825	$0.065_{(5)}$	0.85	6.04	0.82
S_2	0.204	0.354	0.075	1.45	2.59	1.27
S_3^-	0.297	0.646	$0.202_{(5)}$	2.10	4.73	3.61
Molecule (2)						
I,	0.750	-0.154	0.2993	5.501 Å	-1.127 Å	5.956 Å
I₄	0.071	0.579	0.4005	0.451	4.237	7.529
$P_{\overline{a}}$	0.287	0.378	0.454	2.05	2.77	8.69
P_6	0.505	0.387	0.383	3.65	2.83	7.29
\mathbf{P}_{7}	0.307	0.012	0.342	$2 \cdot 24$	0.09	6 ·70
$\mathbf{P_8}$	0.560	-0.059	0.399	4 ·10	-0.43	7.86
\mathbf{S}_4	0.397	0.241	0.297	2.87	1.76	5.69
S_5	0.181	0.116	0.431	1.31	0.82	8.39
\mathbf{S}_{6}	0.665	0.199	$0.431_{(5)}$	4.84	1.46	8.53

theless, for these reflections R was 0.18 and there were no major discrepancies between F_o and F_c . In Table 2 the final atomic coordinates x, y, z are fractions of the unit-cell edges. Also listed are coordinates in Ångström units, X', Y', Z' referred to the orthogonal axes a, b', c where b' is normal to the ac plane, the angle $\beta(90^{\circ} 10')$ being assumed 90° .

5. Accuracy

The two independent values of z found for each atom were used to estimate errors in atomic coordinates. The standard deviation in a coordinate of an iodine atom was estimated to be not greater than 0.01 Å and that of a phosphorus or sulphur atom not greater than 0.03 Å. A calculation by the statistical method of Cruickshank (1949) gave values which were approximately half these estimates and clearly too low, because of the large number of unobserved reflections.



Fig. 2. The molecular configuration of $P_4S_3I_2$, showing the two enantiomorphous molecules of the asymmetric unit. Relative orientations arbitrarily chosen. Assuming the larger estimated values, standard deviations in bond lengths are, 0.032 Å for I-·P bonds and 0.042 Å for P–P and P–S bonds. Standard deviations of bond angles calculated by the method of Cruickshank & Robertson (1953) are $1\cdot1^{\circ}$ for I–P–P and I–P–S angles and $1\cdot7^{\circ}$ for P–S–P, S–P–S and P–P–S angles.

6. Description and discussion of structure

The molecular configuration of phosphorus thioiodide is shown in Fig. 2 and the bond lengths and angles

Table 3.	Bond lengths	$and \ angles$	in $P_4S_3I_2$				
Mole	cule 1	Molecule 2					
$I_1 - P_1$	2·45 Å	$I_3 - P_8$	2·46 Å				
$I_2 - P_4$	2.53	$I_4 - P_9$	2.47				
$P_1 - P_2$	$2 \cdot 23$	$P_5 - P_6$	$2 \cdot 12$				
$P_{3}-P_{4}$	$2 \cdot 19$	$P_7 - P_8$	2.25				
$P_1 - S_1$	2.16	$P_5 - S_5$	2.08				
$P_4 - S_2$	1.99	$P_8 - S_6$	2.14				
$P_3 - S_1$	$2 \cdot 10$	$P_6 - S_6$	$2 \cdot 20$				
$P_2 - S_2$	$2 \cdot 16$	$P_7 - S_5$	2.07				
$P_{2} - S_{3}$	1.99	$P_6 - S_4$	2.08				
P_3-S_3	2.11	$P_7 - S_4$	2.06				
$I_1 - P_1 - S_1$	103°	$I_4 - P_5 - S_5$	104°				
$I_2 - P_4 - S_2$	101	$I_{3} - P_{8} - S_{6}$	107				
$I_{1}-P_{1}-P_{2}$	96	$I_4 - P_5 - P_6$	99				
$I_2 - P_4 - P_3$	98	$I_{3} - P_{8} - P_{7}$	98				
$P_{1} - S_{1} - P_{3}$	106	$\dot{\mathbf{P}_6} - \dot{\mathbf{S}_4} - \dot{\mathbf{P}_7}$	99				
$P_2 - S_2 - P_4$	110	$P_{5} - S_{5} - P_{7}$	107				
$P_2 - S_3 - P_3$	101	$P_6 - S_6 - P_8$	101				
$S_1 - P_3 - S_3$	106	$S_4 - P_6 - S_6$	108				
$S_2 - P_2 - S_3$	102	$S_{4} - P_{7} - S_{5}$	104				
$P_1 - P_2 - S_2$	90	$P_5 - P_6 - S_6$	91				
$P_4 - P_3 - S_1$	92	$P_{8} - P_{7} - S_{5}$	92				
$P_2 - P_1 - S_1$	101	$\tilde{P_6} - P_5 - S_5$	102				
$P_{3} - P_{4} - S_{2}$	101	$P_7 - P_8 - S_6$	104				
$P_1 - P_2 - S_3$	102	$P_8 - P_7 - S_4$	101				
$P_{4}-P_{3}-S_{3}$	102	$\mathbf{P}_{\mathbf{s}} - \mathbf{P}_{\mathbf{s}} - \mathbf{S}_{\mathbf{s}}^{*}$	102				

Table	2.	Atomic	coordinates
10010		110010000	0001 001000000

	P–I (Å)	Р–Р (Å)	P-8 (Å)	S-P-S	P–S–P	P-P-S	Reference
P ₄ S ₃ I ₂ P ₂ I ₄ PI ₃ †	2·48 S.D. 0·032 2·48 0·028 2·52 2·46	2·20 S.D. 0·04 2·21 0·06	2·10 S.D. 0·04	105°	104° 102°, 91°	102°, 91°	a b c d
P_4S_{10} P_4S_7 P_4S_5 P_4S_3 P_4^{\dagger}		$\begin{array}{cccc} 2 \cdot 35 & 0 \cdot 01 \\ 2 \cdot 21 & 0 \cdot 02 \\ 2 \cdot 235 & 0 \cdot 00 \\ 2 \cdot 21 & 0 \cdot 02 \end{array}$	$\begin{array}{cccc} 2 \cdot 085 & 0 \cdot 01 \\ 2 \cdot 08 & 0 \cdot 01 \\ 5 & 2 \cdot 08 - 2 \cdot 19 & 0 \cdot 02 \\ 5 & 2 \cdot 090 & 0 \cdot 00 \end{array}$	109·5° 110°, 103° 5 105°* 5 100°	109·5° 103°* 103°* 103°	102° 104°, 87° 103°	e e, f g h i
Black phosphorus		2.18			Average]	$P-P-P = 102^{\circ}$	j

 Table 4. Average bond lengths (with estimated standard deviations) and angles
 in some phosphorus compounds

* One bond angle observed significantly different from the value indicated. † Electron diffraction.

(a) This analysis; (b) Leung & Waser (1956); (c) Gregg et al. (1937); (d) Hassel & Sandbo (1938); (e) Vos & Wiebenga (1955);
 (f) Vos & Wiebenga (1956); (g) Van Houten & Wiebenga (1957); (h) Leung, Waser et al. (1957); (i) Maxwell et al. (1935);
 (j) Hultgren et al. (1935).

of the two independent molecules are given in Table 3. In Table 4 a comparison is made between the results of this investigation and of the structure determinations of the phosphorus sulphides and iodides and elementary phosphorus.

In the $P_4S_3I_2$ molecule, the phosphorus and sulphur atoms are arranged in two 5-membered rings having a common P-S-P angle. The iodines are bonded to phosphorus atoms in different rings in the cis configuration with respect to the P_4S_3 skeleton. There are three types of bond namely, P-I, P-P and P-S single bonds, averaging 2.48, 2.20, 2.09 Å respectively. There are six different sets of bond angles namely, I-P-P (average value 98°), I-P-S (104°), P-S-P (104°), S-P-S (105°) and two sets of P-P-S angles $(91^{\circ}, 102^{\circ})$, no observed length or angle differing significantly from these average values. The individual molecules show no significant deviations from twofold rotational symmetry and as this is the only molecular symmetry, the crystal structure is composed of pairs of optical isomers related through the centres of symmetry of the space group. The two 5-membered rings are folded about the plane of their common angle ($\angle P_2S_3P_3$, $\angle P_6S_4P_7$) and a measure of this folding is given by the four angles of the type $\angle P_1P_2S_2$ whose average value is 91°. These angles are significantly smaller than the P-P-P angle in black phosphorus (average 102°) and significantly smaller than the other P-P-S angles in the $P_4S_3I_2$ molecule (102°) and any such angle observed in the phosphorus sulphides (except for the value of 88° observed in the unique 4-membered ring in P_4S_5). These small angles are difficult to explain, especially as they give rise to the close non-bonded approaches of the type P_1-S_2 of 3.1 Å, 0.6 Å lower than the sum of van der Waals radii (Pauling, 1940).

The arrangement of the molecules in the crystal is shown in Fig. 3. The closest approach of iodine atoms is that of 3.90 Å between atoms of the type I_2 and I_3 , as compared with 3.54 Å the closest non-bonded



Fig. 3. Views of the arrangement of molecules (a) along the b axis, (b) along the a axis.

approach in crystalline iodine (Harris, Mack & Blake, 1928). Other intermolecular distances in $P_4S_3I_2$ are not less than 3.7 Å.



Fig. 4. The molecular configurations of P_4S_3 and $P_4S_3I_2$.

A comparison of the molecular configurations of $P_4S_3I_2$ and P_4S_3 (Fig. 4) provides further convincing evidence for the high mobility of P-P and P-S bonds. Although $P_4S_3I_2$ may be prepared from P_4S_3 by reaction with iodine in carbon disulphide, a reaction which proceeds readily, a rearrangement of the atoms of the P_4S_3 skeleton takes place during the process. As well as a P-P bond being broken, the positions of a phosphorus and a sulphur atom in one of the 5-membered rings are reversed.

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